## Experiment 6 Linear motion and Newton's second law

## 1-Objects of the experiment:

- Measuring the time required by a trolley of mass $m_{1}$ to cover a certain path " $d$ ".
- Representing the relation between path and time in an d- $\mathrm{t}^{2}$ diagram.
- Calculating the acceleration "a" of the trolley of mass $m_{l}$ with different masses of the falling object of mass $m_{2}$.


## 2-Principles



Figure 1.
If the acceleration is constant, we can use the following kinematics equation:

$$
\begin{equation*}
d=v_{0} t+\frac{1}{2} a t^{2} \tag{1}
\end{equation*}
$$

$v_{0}=v_{A}=0$, then

$$
\begin{equation*}
d=\frac{1}{2} a t^{2} \tag{2}
\end{equation*}
$$

Rearrangement of Equation 2 gives us:

$$
\begin{equation*}
t^{2}=\frac{2}{a} d \tag{3}
\end{equation*}
$$

The Newton's second law:

$$
\begin{equation*}
\sum \vec{F}=m_{1} \vec{a} \tag{4}
\end{equation*}
$$

where $\sum \vec{F}$ is the resultant force exerted on the mass $\mathrm{m}_{1}$ (or $\mathrm{m}_{2}$ ) and $\vec{a}$ is its acceleration.


Two masses connected by a light cord.


Fig. 2: Free- body diagrams for the two masses:

By using (Equation 4), we can find the acceleration as:

$$
\begin{equation*}
a=\frac{m_{2}}{m_{1}+m_{2}} g \tag{5}
\end{equation*}
$$

## 3-Carrying out the experiment

- Align the track horizontally.
- Adjust the voltage at the holding magnet so that the trolley with the additional weight is just held.
- Define the starting point with the movable interrupter flag on the trolley, and read it from the scale of the track.
- Position the light barrier at a distance of 20 cm from the starting point.
- Release the motion by pressing the START/STOP key at the stopclock.
- Wait until the interrupter flag passes the light barrier, and read the time from the stopclock.
- Reset the stopclock to zero by pressing the RESET key.
- Repeat the measurement at distances $30 \mathrm{~cm}, 40 \mathrm{~cm}, 50 \mathrm{~cm}$, and 60 cm from the starting point.


## 4-Measurements

Table 1. Distance as a function of time with $\mathbf{m}_{\mathbf{1}}=\mathbf{0 . 4 8 6 k g}$ and $\mathbf{m}_{\mathbf{2}}=\mathbf{0} \mathbf{0 . 0 2 5 2 k g}$.

| $\boldsymbol{d}(\boldsymbol{m})$ | $\boldsymbol{t}_{\boldsymbol{1}}(\boldsymbol{s})$ | $\boldsymbol{t}_{\mathbf{2}}(\boldsymbol{s})$ | $\boldsymbol{t}_{\mathbf{3}}(\boldsymbol{s})$ | Average $\boldsymbol{t}$ | $\boldsymbol{t}^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0.2 |  |  |  |  |  |
| 0.3 |  |  |  |  |  |
| 0.4 |  |  |  |  |  |
| 0.5 |  |  |  |  |  |
| 0.6 |  |  |  |  |  |

- Graph distance $\mathbf{d}$ versus time squared $\mathbf{t}^{\mathbf{2}}$ (d is the axis-x and $\mathrm{t}^{2}$ is the axis-y)
- Draw the best line.
- Determine the acceleration " $a$ " by finding a relation between the slope and the acceleration (use Equation 3).
- Determine the acceleration " $\boldsymbol{a}$ " by repeating the measurement as above but with $\mathrm{m}_{2}=$ 0.0452 kg .

Table 2. Distance as a function of time with $\mathbf{m}_{\mathbf{1}}=\mathbf{0 . 4 8 6} \mathrm{kg}$ and $\mathbf{m}_{\mathbf{2}}=\mathbf{0} \mathbf{0} \mathbf{0 4 5 2} \mathbf{k g}$.

| $\boldsymbol{d}(\mathrm{m})$ | $\boldsymbol{t}_{\mathbf{1}}(\boldsymbol{s})$ | $\boldsymbol{t}_{\mathbf{2}}(\boldsymbol{s})$ | $\boldsymbol{t}_{\mathbf{3}}(\boldsymbol{s})$ | Average $\boldsymbol{t}$ | $\boldsymbol{t}^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0.2 |  |  |  |  |  |
| 0.3 |  |  |  |  |  |
| 0.4 |  |  |  |  |  |
| 0.5 |  |  |  |  |  |
| 0.6 |  |  |  |  |  |

- Discuss your results.

