



Department: Mathematics & Statistics  
Semester/Year: First /1435-1436  
Duration: 75 minutes

Course Elements of sets and structures  
Course Code: MAT 220

Midterm 2

**QUESTION 1 [10=4+4x1.5 marks]**

1. Let  $U = \{1, 2, 3, \dots, 10\}$ ,  $A = \{x \in U \mid x \text{ is even}\}$ ,  $B = \{x \in U \mid x \text{ is odd}\}$  and  $C = \{1, 2, 4\}$ ,  
Determine (a)  $(A \cap C)'$  (b)  $(A \cup B)'$  (c)  $A - C$  (d)  $P(C)$ , the power set of C

2. Prove or disprove the following, where A, B, C and D are subsets of the universal set U:

- (i) If  $A \cap C \subseteq B \cap C$ , then  $A \subseteq B$ .
- (ii) If  $A \subseteq B$ , then  $B' \subseteq A'$ .
- (iii) If  $A \times C = B \times C$ , then  $A = B$ .
- (iv) If  $A \subseteq B$  and  $C \subseteq D$ , then  $A \cup C \subseteq B \cup D$ .

**QUESTION 2 [5=5+5 marks]**

1. Let R and S be two relations defined on the set  $A = \{1, 2, 3, 4, 5\}$  as follows  $R = \{(x, y) \mid x < y\}$ ,  
 $S = \{(x, y) \mid x + y \text{ is prime}\}$ . Determine (a) Dom (R) and Rng(S), (b)  $S \circ R$  (c)  $R^{-1} \circ S^{-1}$   
(d) Which of R or S is symmetric? (e) Which of R or S is transitive?

2. Let R be a relation defined on  $\mathbb{Z}$  as follows:  $(x, y) \in R \Leftrightarrow x \equiv y \pmod{3}$ .

- (i) Show that R is an equivalence relation on  $\mathbb{Z}$
- (ii) Find the equivalence classes of R and the partition of  $\mathbb{Z}$  by R.
- (iii) Is R a relation of order?.

3.

**Extra exercise (bonus) [ 2 marks ]:**

Let A, B and C be subsets of the universal set U. Prove that  $A - B = A \cap B'$  and use this to show that:  $(A - B) - C = (A - C) - (B - C)$