

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

Kingdom of Saudi Arabia
Ministry of Higher Education
Al-Imam Mohammed Ibn Saud
Islamic University
- College of Science -
Department: Maths & Stat.
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Duration: 2 hours



المملكة العربية السعودية
وزارة التعليم العالي
جامعة الإمام محمد بن سعود الإسلامية
- كلية العلوم -
Course Name: Applied Cal. 1
Course Code: MAT 113
Coordinator:

FINAL EXAM

Question 1. [2+2+2+2+2=10 marks]

1) Evaluate each of the following limits:

$$a) \lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1+x^2}}{x}, \quad b) \lim_{x \rightarrow 1} \frac{\ln(2-x^2)}{x^2-x},$$

$$c) \lim_{x \rightarrow -\infty} \frac{\sqrt{9x^2-1}}{3x+5}, \quad d) \lim_{x \rightarrow 0} x \csc(2x).$$

2) Find all vertical and horizontal asymptotes of the function $f(x) = \frac{2x^2+1}{x^2+x-6}$.

Question 2. [2+2+2+2+2=10 marks]

1) Compute the derivatives of the following functions:

$$a) f(x) = \sqrt{\sin^2 x + 3} - \ln(x^2 - 3x), \quad b) g(x) = \frac{e^{x^2} + x}{\sqrt{x}}.$$

2) Find the equation of the tangent line to the graph of $f(x) = (2x^3 + 3)(x - 1)$ at $a = 1$.

3) Use implicit differentiation to find y' if $y^4 + xy^2 - 5y = 3x$.

4) Verify the conditions of Rolle's theorem and find all values of c satisfying the conclusion of it for the function $f(x) = x^4 - 2x^2$ on $[-2, 2]$.

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Question 3. [2+2+3+1+3+1=12 marks]

Consider the function f defined by $f(x) = x^3 + 3x^2 - 4$.

- 1) Find the critical numbers of the function f .
- 2) Find the absolute extrema of the function f on the interval $[-1, 1]$.
- 3) Determine the intervals on which the function f is increasing and the ones where f is decreasing.
- 4) Find the local extrema of the function f .
- 5) Determine the intervals where the graph of f is concave up and the ones where it is concave down.
- 6) Find the inflection point of the graph of f .

Question 4. [2+2+2+2=8 marks]

Evaluate each of the following integrals:

$$\begin{array}{ll} a) \int \frac{(\sqrt{x} + 2)^2}{\sqrt{x}} dx, & b) \int x\sqrt{x+4} dx. \\ c) \int_1^2 \frac{xe^{3x} - 2}{x} dx, & d) \int_0^1 x \cos(\pi x^2) dx. \end{array}$$