

**Calculus II, MAT102,**  
**Sheet 2 (TRIGONOMETRIC TECHNIQUES OF & INTEGRATION OF RA-**  
**TIONAL FUNCTIONS USING PARTIAL FRACTIONS)**

Name	
Student Number	
Year	
Mark	/10
Hand in by	

**(Exercises)**

*Please attach your working, with this sheet at the front.*

1. Evaluate the following integrals

$$\begin{aligned}
 \text{(i)} \quad & \int \cos^3 x \sin^4 x \, dx \\
 \text{(ii)} \quad & \int_{\frac{\pi}{4}}^{\frac{\pi}{3}} \cos^3 3x \sin^3 3x \, dx \\
 \text{(iii)} \quad & \int \tan x \sec^3 x \, dx \\
 \text{(iv)} \quad & \int \cos^2 x \sin^2 x \, dx \\
 \text{(v)} \quad & \int \frac{x}{\sqrt{x^2 - 4}} \, dx \\
 \text{(vi)} \quad & \int \frac{x^2}{\sqrt{9 + x^2}} \, dx \\
 \text{(vi)} \quad & \int x^2 \sqrt{x^2 + 9} \, dx \\
 \text{(vii)} \quad & \int \frac{x+1}{\sqrt{4+x^2}} \, dx
 \end{aligned}$$

2. Evaluate the following integrals using a partial fractions

$$\begin{aligned}
 \text{(i)} \quad & \int \frac{5x-2}{x^4-1} \, dx \\
 \text{(ii)} \quad & \int \frac{3x}{x^2-3x-4} \, dx \\
 \text{(iii)} \quad & \int \frac{x+2}{x^3+x} \, dx
 \end{aligned}$$

$$(\text{v}) \int \frac{x^3 + x}{x^2 - 1} dx$$

$$(\text{vi}) \int \frac{x^3 + x + 2}{x^2 + 2x - 8} dx$$

$$(\text{vii}) \int \frac{x + 4}{x^3 + 3x^2 + 2x} dx .$$